

NS8-53: Percents

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A **percent** is a ratio that compares a number to 100. The term "percent" means "out of 100" or "for every 100." For instance, 84% on a test means 84 out of 100.

You can think of percent as a short form for a fraction with 100 in the denominator:

$$\text{Example: } 45\% = \frac{45}{100}$$

1. Write the following percents as fractions:

a) 17%

b) 34%

c) 10%

d) 29%

e) 45%

f) 100%

g) 1%

h) 80%

2. Write the following fractions as percents:

a) $\frac{50}{100}$

b) $\frac{46}{100}$

c) $\frac{62}{100}$

d) $\frac{100}{100}$

e) $\frac{25}{100}$

f) $\frac{99}{100}$

g) $\frac{90}{100}$

h) $\frac{1}{100}$

3. Write the following decimals as percents, by first turning them into fractions. The first one has been done for you:

a) $.72 = \frac{72}{100} = 72\%$

b) .54

c) .09

4. Write the fraction as a percent by changing it to a fraction over 100. The first one has been done for you:

a) $\frac{3 \times 20}{5 \times 20} = \frac{60}{100} = 60\%$

b) $\frac{4}{5}$

c) $\frac{5}{5}$

d) $\frac{9}{10}$

e) $\frac{3}{4}$

f) $\frac{1}{2}$

g) $\frac{1}{10}$

h) $\frac{3}{20}$

i) $\frac{13}{20}$

j) $\frac{8}{25}$

k) $\frac{18}{25}$

l) $\frac{24}{25}$

m) $\frac{37}{50}$

n) $\frac{43}{50}$

5. Write the following decimals as percents. The first one has been done for you:

a) $.2 = \frac{2}{10} \times \frac{10}{10} = \frac{20}{100} = 20\%$

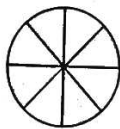
b) $.3$

c) $.4$

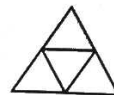
d) $.8$

6. What percent of the figure is shaded?

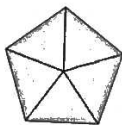
a)



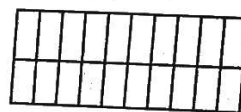
b)



c)



d)



7. Change the following fractions to percents by first reducing them to lowest terms:

a) $\frac{9}{15} \div 3 = \frac{3}{5} = \frac{3}{5} \times \frac{20}{20} = \frac{60}{100} = 60\%$

b) $\frac{3}{15}$

c) $\frac{9}{18}$

d) $\frac{6}{24}$

e) $\frac{24}{32}$

f) $\frac{36}{45}$

g) $\frac{24}{60}$

h) $\frac{22}{40}$

i) $\frac{32}{80}$

j) $\frac{28}{56}$

k) $\frac{75}{150}$

l) $\frac{60}{75}$

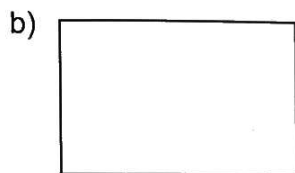
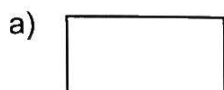
NS8-54: Visual Representations of Percents

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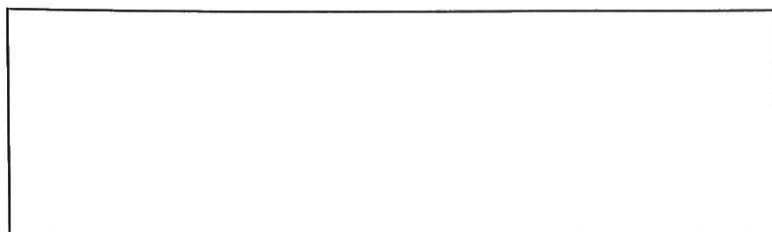
1. Fill in the chart below. The first one has been done for you:

Drawing				
Fraction	$\frac{23}{100}$	$\frac{\quad}{100}$	$\frac{35}{100}$	$\frac{\quad}{100}$
Decimal	0.23	0.____	0.____	0.39
Percent	23%	74%	____ %	____ %

2. Shade 50% of each box:



3. Colour 50% of the rectangle blue, 30% red, and 20% green:

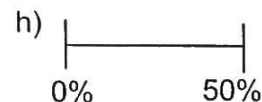
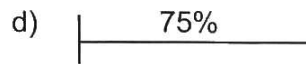
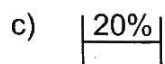
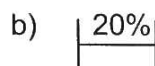
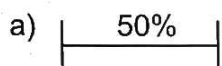


4. Write a fraction for each part shaded. Then write the fraction with a denominator of 100. Then write a decimal and a percent for each:

a) Fraction $\frac{\quad}{\quad}$
 Fraction with denominator 100 $\frac{\quad}{100}$
 decimal _____ percent _____

b) Fraction $\frac{\quad}{\quad}$
 Fraction with denominator 100 $\frac{\quad}{100}$
 decimal _____ percent _____

5. Extend each line segment to show 100%:



1. Write < or > or = between the following pairs of numbers. First change each pair of numbers to a pair of fractions with the same denominator. The first one is done for you:

a)

$\frac{1}{2}$	47%
$\frac{50 \times 1}{50 \times 2}$	$\frac{47}{100}$
$\frac{50}{100}$	$\frac{47}{100}$

b)

$\frac{1}{2}$	49%

c)

$\frac{3}{5}$	66%

d)

.37	73%

e)

.02	20%

f)

$\frac{1}{10}$	10%

g)

$\frac{19}{20}$	98%

h)

$\frac{27}{50}$	54%

i)

.9	9%

j)

$\frac{17}{25}$	68%

k)

$\frac{13}{20}$	65%

l)

.42	43%

2. Complete the charts.

Fraction	Decimal	Percent
$\frac{2}{5}$		
	.75	
$\frac{11}{20}$		
		70%

Fraction	Decimal	Percent
	.30	
$\frac{12}{16}$		
		25%
	.65	

3. In your notebook, write each set of numbers in order from least to greatest, by first changing each number to a fraction.

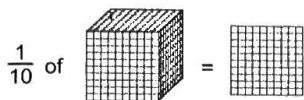
a) $\frac{1}{5}$, 22% , .15

b) $\frac{1}{4}$, .50 , 43%

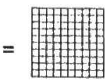
c) $\frac{1}{10}$, .01 , 15%

d) $\frac{2}{3}$, 60% , .57

If you use a thousands cube to represent 1 whole, you can see that taking $\frac{1}{10}$ of a number is the same as dividing by 10 (the decimal shifts one place left):



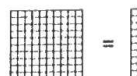
$\frac{1}{10}$ of



=

$$\frac{1}{10} \text{ of } 1 = .1$$

$\frac{1}{10}$ of



=

$$\frac{1}{10} \text{ of } .1 = .01$$

$\frac{1}{10}$ of



=

$$\frac{1}{10} \text{ of } .01 = .001$$

1. Find $\frac{1}{10}$ of the following numbers by shifting the decimal. Write your answers in the boxes provided:

a) 7

b) 10

c) 35

d) 210

e) 6.4

f) 50.6

2. 10% is short for $\frac{10}{100}$ or $\frac{1}{10}$. Find 10% of the following numbers:

a) 1

b) 3.9

c) 4.05

d) 6.74

e) .09

f) 60.08

3. You can find percents that are multiples of 10 as follows:

Example: Finding 30% of 21 is the same as finding 10% of 21 and multiplying the result by 3:

Step 1 10% of 21 =

Step 2 $3 \times$ = 6.3

So 30% of 21 = 6.3.

Find the percents using the method above:

a) 30% of 15

b) 50% of 24

c) 20% of 7.8

i) 10% of 15 =

i) 10% of =

i) 10% of =

ii) $3 \times$ =

ii) \times =

ii) \times =

d) 40% of 75

e) 90% of 86

f) 80% of .5

i) 10% of =

i) 10% of =

i) 10% of =

ii) \times =

ii) \times =

ii) \times =

NS8-57: Finding Percents (Advanced)

35% is short for $\frac{35}{100}$. To find 35% of 27, Sadie finds $\frac{35}{100}$ of 27.

Step 1 She multiplies 27 by 35.

2	3	
	2	7
x	3	5
1	3	5
8	1	0
9	4	5

Step 2 She divides the result by 100.

$$945 \div 100 = 9.45$$

So 35% of 27 is 9.45.

1. Find the following percents using Sadie's method:

a) 25% of 44

Step 1:

x		

Step 2:

$$\underline{\hspace{2cm}} \div 100 =$$

So of is .

b) 18% of 92

Step 1:

x		

Step 2:

$$\underline{\hspace{2cm}} \div 100 =$$

So of is .

Answer the following questions in your notebook.

2. Find the following percents using Sadie's method:

a) 23% of 23

b) 15% of 26

c) 26% of 15

d) 64% of 58

e) 58% of 64

f) 50% of 81

g) 81% of 50

h) 92% of 11

3. 25% is equal to $\frac{1}{4}$ and 75% is equal to $\frac{3}{4}$. Find:

a) 25% of 80

b) 25% of 28

c) 25% of 156

d) 75% of 60

e) 75% of 244

2. 3 is what percent of 20? You can find out by writing a ratio. Write a ratio to answer the following questions:

HINT: You will have to reduce some ratios.

<p>The part goes here → $\frac{3}{20} = \frac{?}{100} \Rightarrow \frac{3}{20} = \frac{15}{100}$</p> <p>The whole goes here →</p> <p>So 3 is 15% of 20.</p>
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- a) 5 is what percent of 25? b) 17 is what percent of 20? c) 4 is what percent of 5?
d) 7 is what percent of 14? e) 16 is what percent of 48? f) What percent of 20 is 13?

3. Students in a class were asked to choose one sport to participate in for a sports day:

- a) Complete the chart.
b) How many students are in the class?

Sport	Fraction of Class that chose the sport	Percent	Decimal	Number of Students that chose the sport
Soccer	$\frac{1}{5}$			4
Swimming		40 %		
Baseball				
Gymnastics			.15	

4. Find each amount by using a ratio or decimal multiplication:

- a) What is 22% of 70? b) What is 15% of 9? c) What percent of 50 is 10?
d) What percent of 20 is 9? e) What percent of 25 is 6? f) What is 18% of 42%?

5. Grasslands make up 2.5% of the habitat of birds in North America; 2.5% is short for $\frac{2.5}{100}$.

If you multiply the numerator and denominator by 10, you get a proper fraction: $\frac{2.5 \times 10}{100 \times 10} = \frac{25}{1000} = \frac{1}{40}$

Express each percent as a proper fraction and reduce to lowest terms:

- a) 17.5% b) .7% c) 6.4% d) .04%

6. a) Change the following decimals to percents:

i) $.235 = \frac{235}{1000} = \frac{235 \div 10}{1000 \div 10} = \frac{23.5}{100} = 23.5\%$ ii) .273 iii) .848 iv) .369

- b) Change the following fractions to decimals by long division. Express your answers as percents:

i) $\frac{7}{20}$ ii) $\frac{11}{20}$ iii) $\frac{3}{8}$ iv) $\frac{5}{8}$

7. After a 10% discount, a book costs \$27.00. How much does the book cost without the discount?